

# Quartz Crystal Resonator with a Superhydrophobic Surface

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Acknowledgements: EPSRC

# Overview

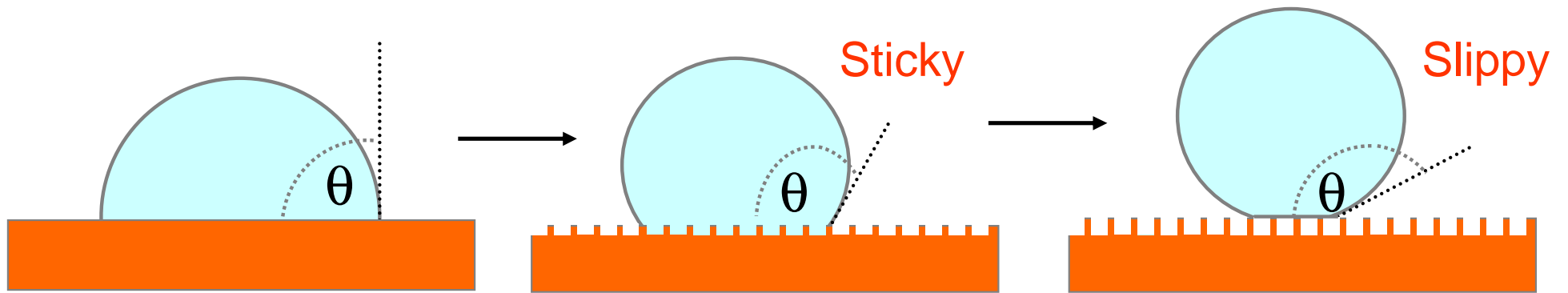
1. Superhydrophobicity & Slip
2. QCM Surfaces
3. Data for Superhydrophobic QCM
4. Conclusions

# Superhydrophobicity and Slip

# Topography & Wetting

## Droplets that Skate

What contact angle does a droplet adopt on a “rough” surface?



Young's Law

$$\cos \theta_e = (\gamma_{SV} - \gamma_{SL}) / \gamma_{LV}$$

Wenzel Eq.

$$\cos \theta_{CB} = r \cos \theta_e$$

Cassie-Baxter Eq

$$\cos \theta_{CB} = f_s \cos \theta_e - (1 - f_s)$$

Roughness

Chemistry

Young's Law  $\theta_e$

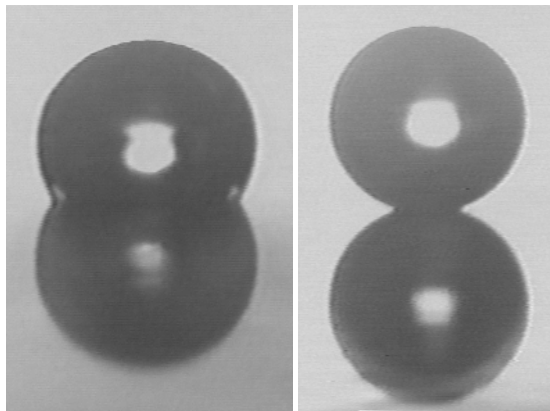
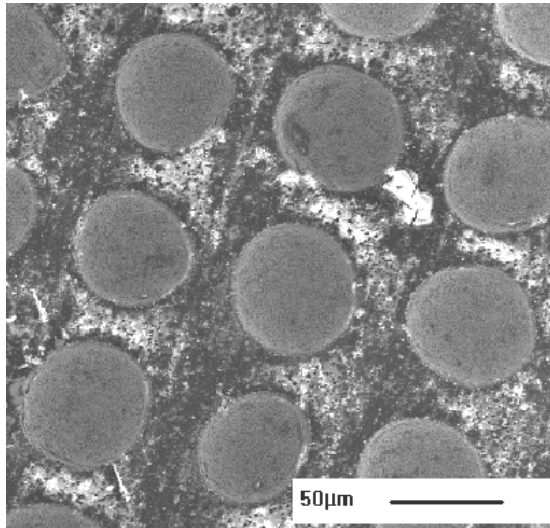
Topography

$r$  = true area/planar projection

$f_s$  = solid surface fraction

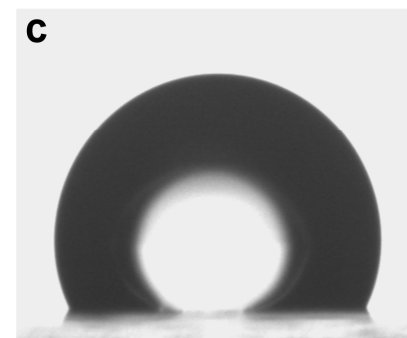
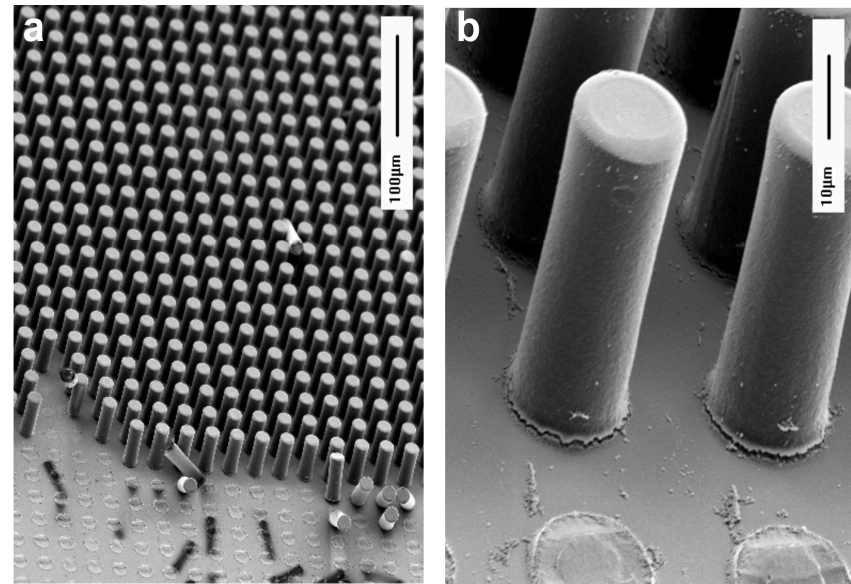
# Topographic Enhancement of Water Repellence

## Etched Metal

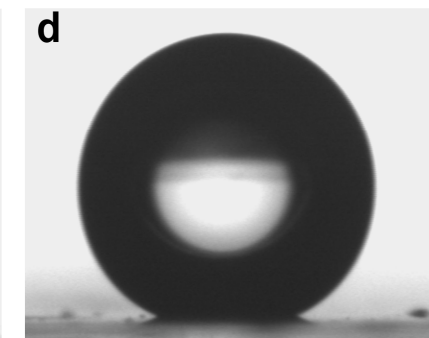


Flat & hydrophobic      Patterned & hydrophobic

## Polymer Microposts



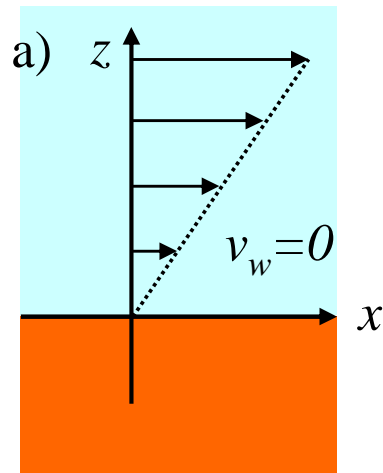
Flat & hydrophobic



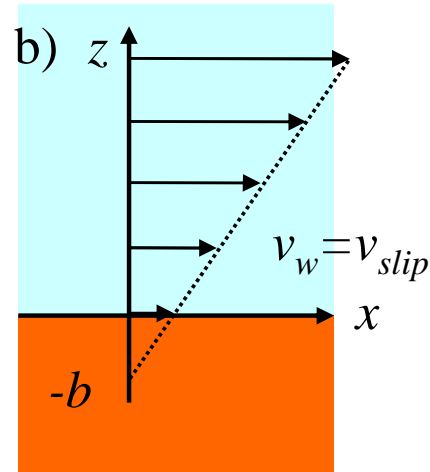
Patterned & hydrophobic

# Slip by Simple Newtonian Liquids

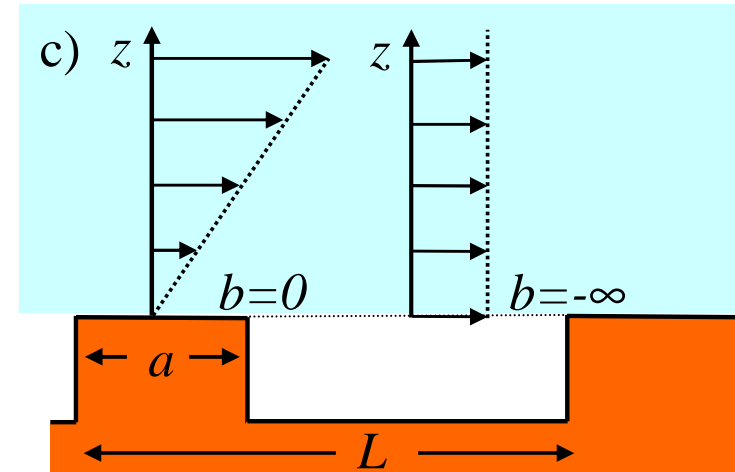
## No Slip



## Slip



## Mixed



## Experimental Evidence – Steady Flow

1. Theory<sup>1,2</sup> supported by simulations suggests  $b=L f(\varphi_s)/2\pi$
2. Micro-PIV experiments detailing flow profiles<sup>3</sup> ( $h=1-7 \mu\text{m} \Rightarrow b=0.28L$ )
3. Cone-and-plate rheometer experiments<sup>4</sup> – drag reduction  $> 10\%$
4. Hydrofoil in a water tunnel experiments<sup>5</sup> – drag reduction of  $10\%$

# QCM Surfaces

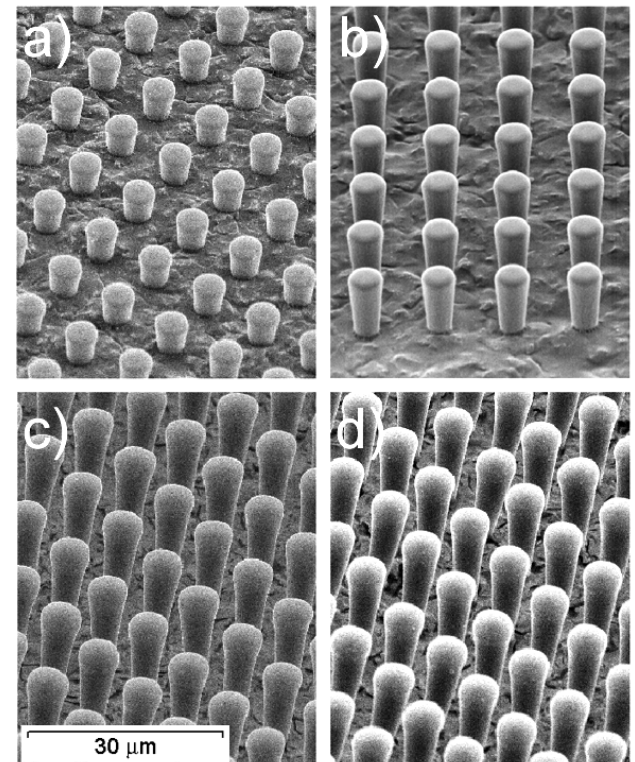
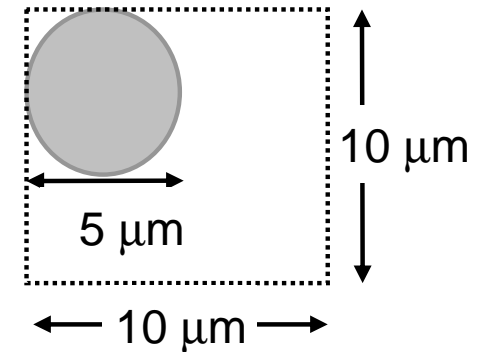
# QCM with Micro-Post Textures

## Previous Data on QCMs

1. Polyethylene glycol-water on a hydrophobic micro-post QCM<sup>1</sup>
2. Polystyrene with embedded PTFE based superhydrophobic surface<sup>2</sup>
3. 0.6  $\mu\text{m}$  silica nanoparticle layer superhydrophobic multiresonance device<sup>3</sup>

## New Experiments in this Talk

1. SU-8 micro-posts 5, 10, 15, 18  $\mu\text{m}$  tall
2. Water-glycerol mixtures (0-100%)
3. Bare (non-hydrophobised) & hydrophobised
4. Contact angles
5. Impedance spectra fitted to BVD model





# Contact Angle Data

Concentrations:	0%	40%	51.3%	58.2%	69.2%	78.2%
Bare flat SU-8, $\theta_s$	75°	69°	73°	66°	68°	65°
Hydrophobic flat, $\theta_s^H$	115°	113°	105°	109°	100°	111°
<hr/>						
Bare 5 $\mu\text{m}$ post, $\theta$	106°	101°	95°	96°	88°	86°
Hydrophobic 5 $\mu\text{m}$ post, $\theta^H$	155°	150°	152°	149°	152°	151°
Bare 10 $\mu\text{m}$ post, $\theta$	118°	121°	109°	111°	103°	99°
Hydrophobic 10 $\mu\text{m}$ post, $\theta^H$	151°	148°	147°	148°	151°	149°
Bare 15 $\mu\text{m}$ post, $\theta$	119°	127°	117°	95°	115°	118°
Hydrophobic 15 $\mu\text{m}$ post, $\theta^H$	143°	149°	143°	147°	144°	148°
Bare 18 $\mu\text{m}$ post, $\theta$	123°	117°	113°	120°	106°	116°
Hydrophobic 18 $\mu\text{m}$ post, $\theta^H$	138°	149°	138°	148°	137°	150°

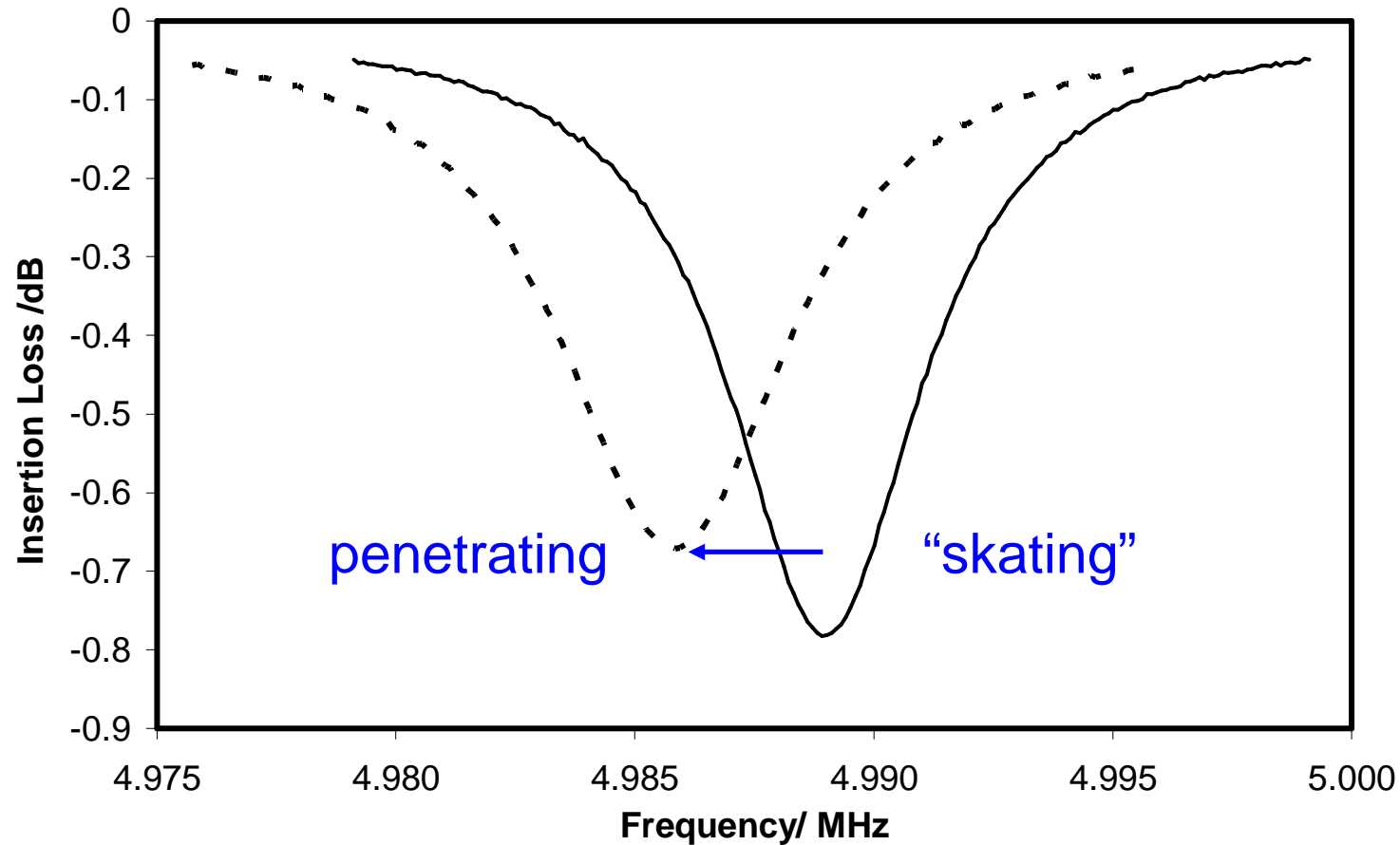
## Cassie-Baxter Theory

Bare posts should give  $(138 \pm 2)^\circ$

Hydrophobic posts should be  $(150 \pm 3)^\circ$

1. *Partial penetration of bare posts*
2. *“Skating” on hydrophobised posts*

# QCM Confirmation of “Skating”



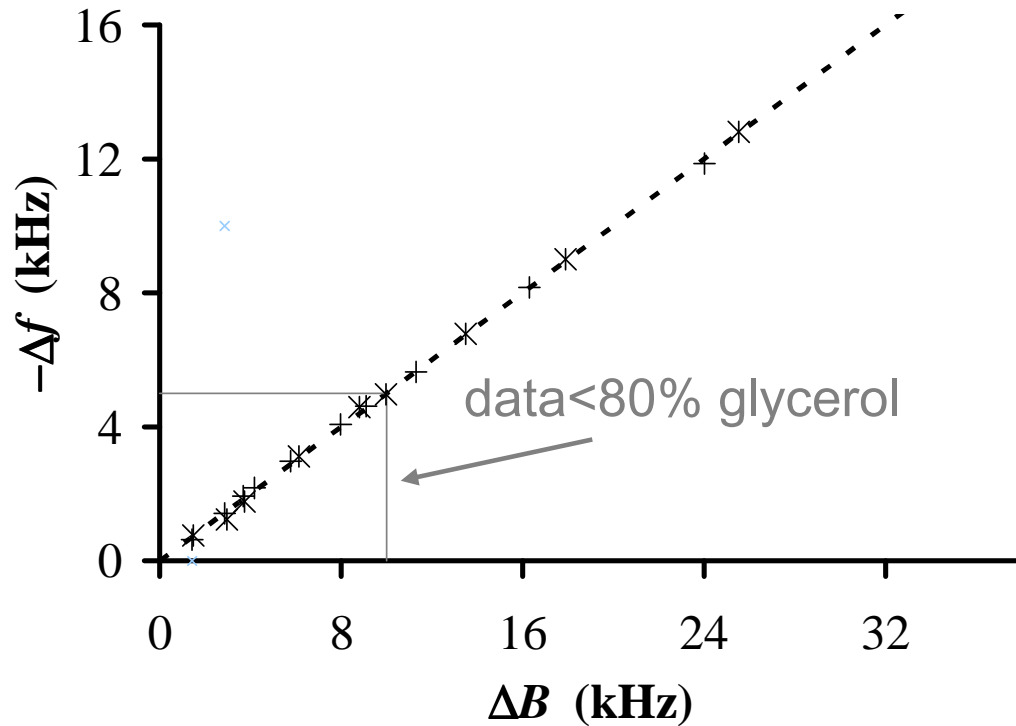
Hydrophobised 18  $\mu\text{m}$  micro-posts  
Solid-line is before pressure applied  
Dotted curves is after pressure is applied

Visually confirmed water ingress  
after pressure applied

# Data for Superhydrophobic QCM's

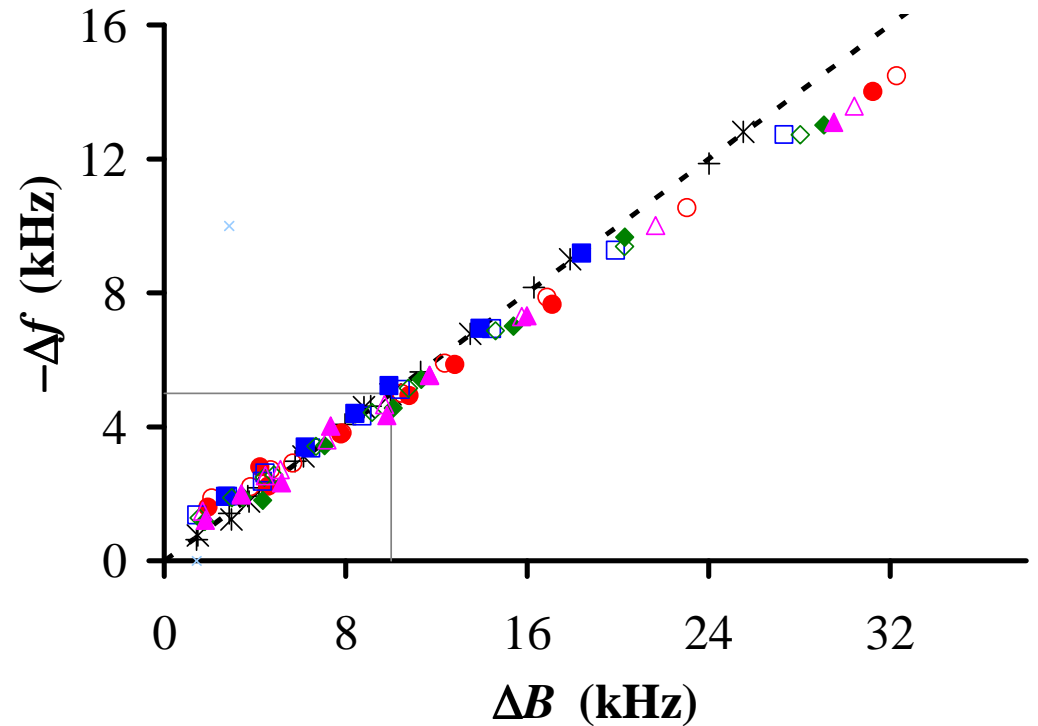
# Flat Surfaces – Newtonian Liquid

## Polished Crystal



Bare (non-hydrophobised) = +++  
 Hydrophobised = \*\*\*  
 Kanazawa & Gordon Theory = - - - -

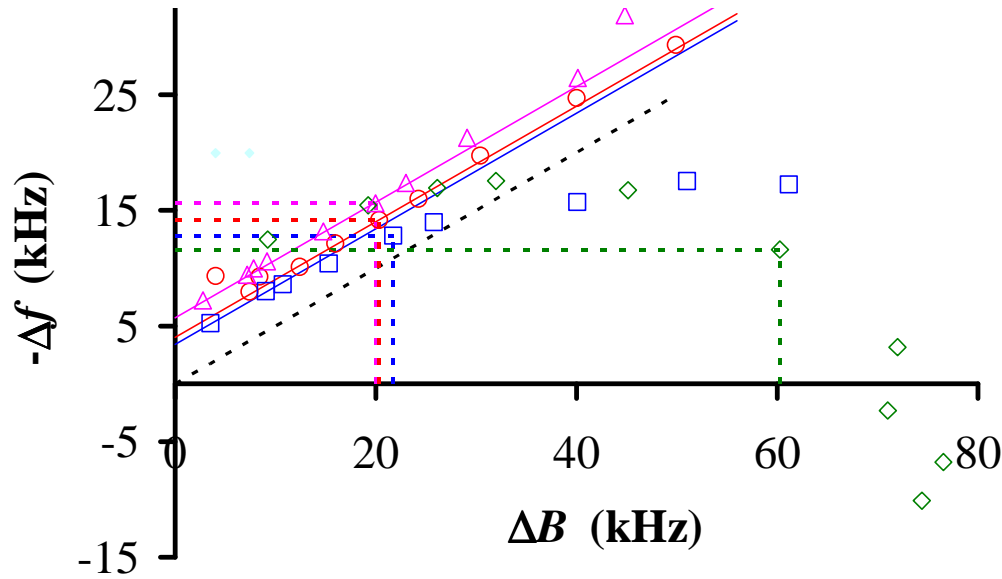
## Spin Coated SU-8



5 $\mu$ m = □□□      10 $\mu$ m = ◇◇◇  
 15 $\mu$ m = △△△      18 $\mu$ m = ○○○  
 Filled symbols = hydrophobised

# Micro-Post Surfaces – Newtonian or Not?

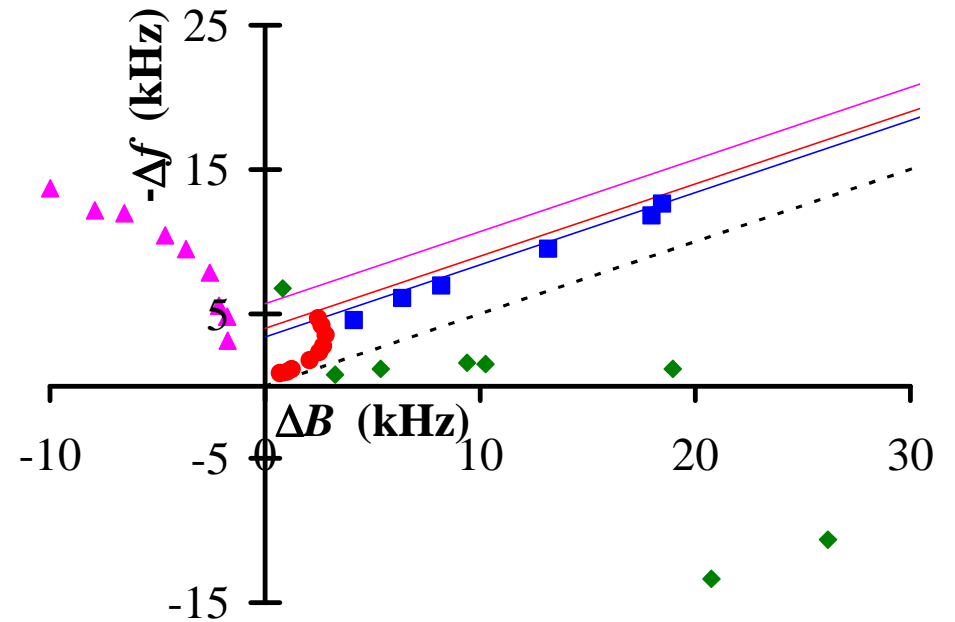
## Bare (non-hydrophobised)



$5\mu\text{m}$  =  $\square\square\square$        $10\mu\text{m}$  =  $\diamond\diamond\diamond$   
 $15\mu\text{m}$  =  $\triangle\triangle\triangle$        $18\mu\text{m}$  =  $\circ\circ\circ$   
 Filled symbols = hydrophobised

Data < 80% glycerol = dotted rectangles  
 Kanazawa & Gordon Theory = - - - -  
 Solid lines = Guide to eye for 0.5 slope

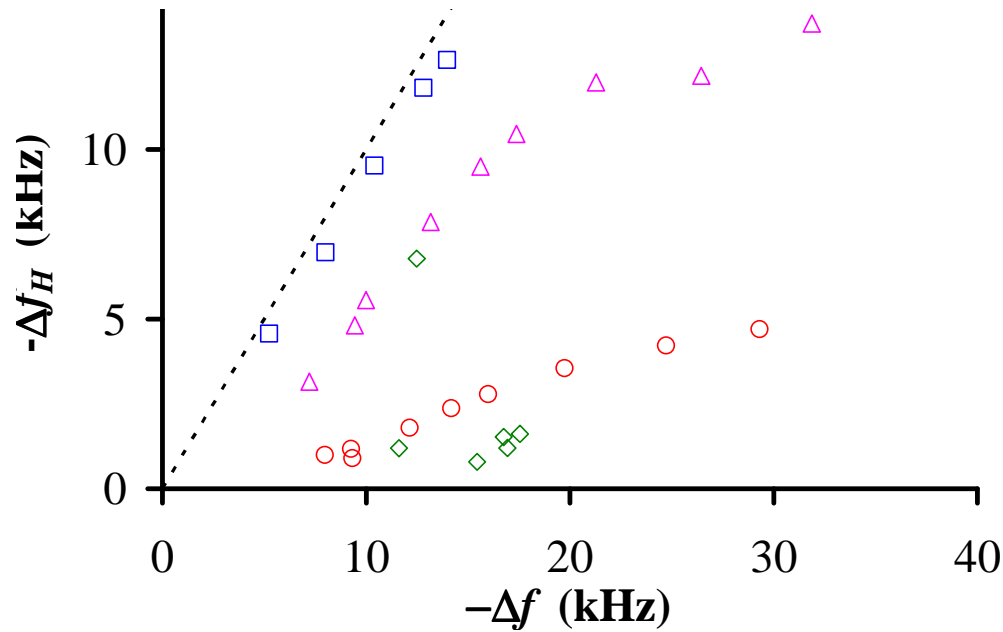
## Hydrophobised



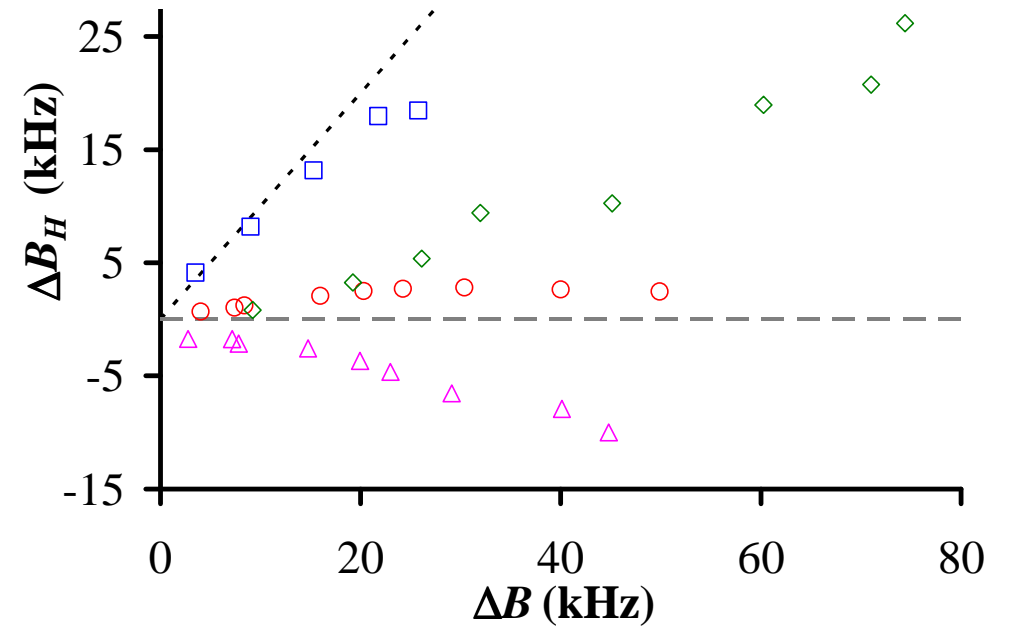
*Hydrophobisation of taller posts  
changes type of response*

# Micro-Post Surfaces: Hydrophobised v Bare

Frequency



Bandwidth



5  $\mu\text{m}$  =  $\square\square\square$

10  $\mu\text{m}$  =  $\diamond\diamond\diamond$

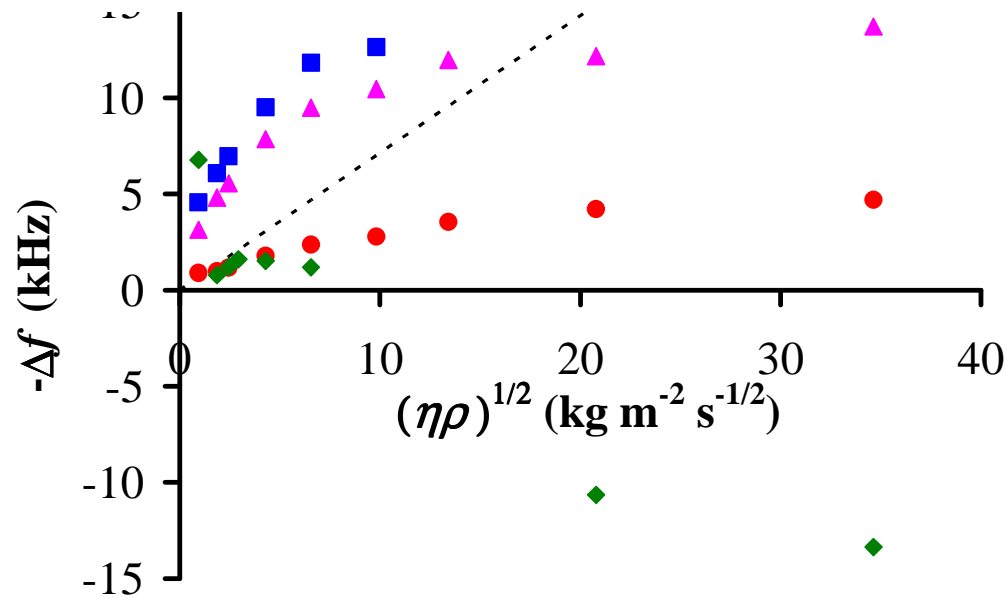
15  $\mu\text{m}$  =  $\triangle\triangle\triangle$

18  $\mu\text{m}$  =  $\circ\circ\circ$

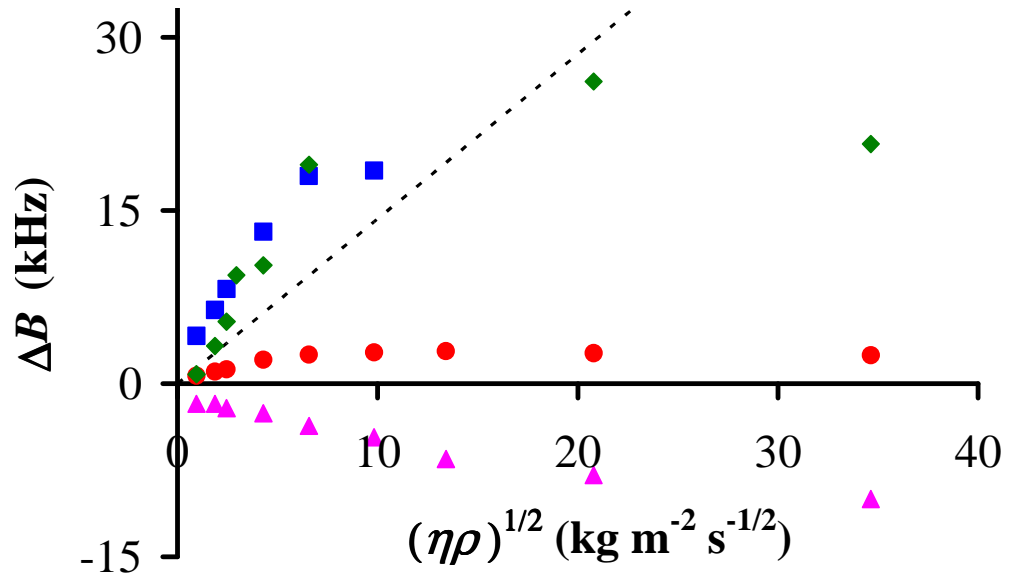
*Taller hydrophobic posts decouple response from liquid*

# Micro-Post Surfaces: Viscosity-Density

Frequency



Bandwidth



5  $\mu\text{m}$  =  $\square\square\square$

10  $\mu\text{m}$  =  $\diamond\diamond\diamond$

Filled symbols = hydrophobised

15  $\mu\text{m}$  =  $\triangle\triangle\triangle$

18  $\mu\text{m}$  =  $\circ\circ\circ$

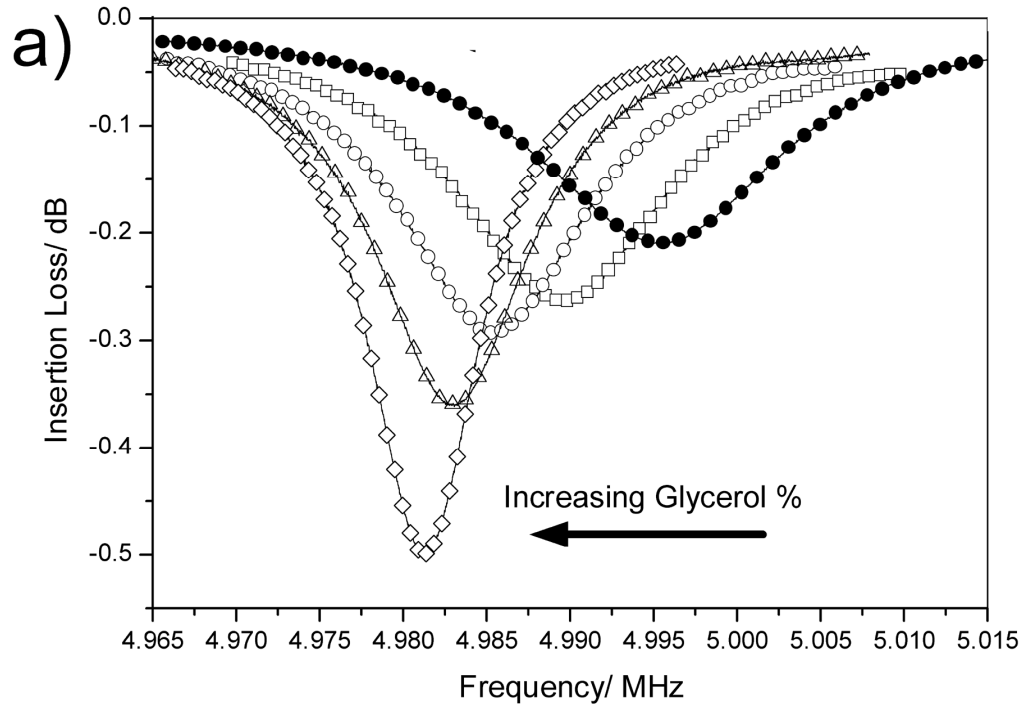
Kanazawa & Gordon Theory = - - - -

*Tallest (18  $\mu\text{m}$ ) hydrophobic posts have reduced coupling to liquid*

*10  $\mu\text{m}$  and 15  $\mu\text{m}$  tall posts have unusual response*

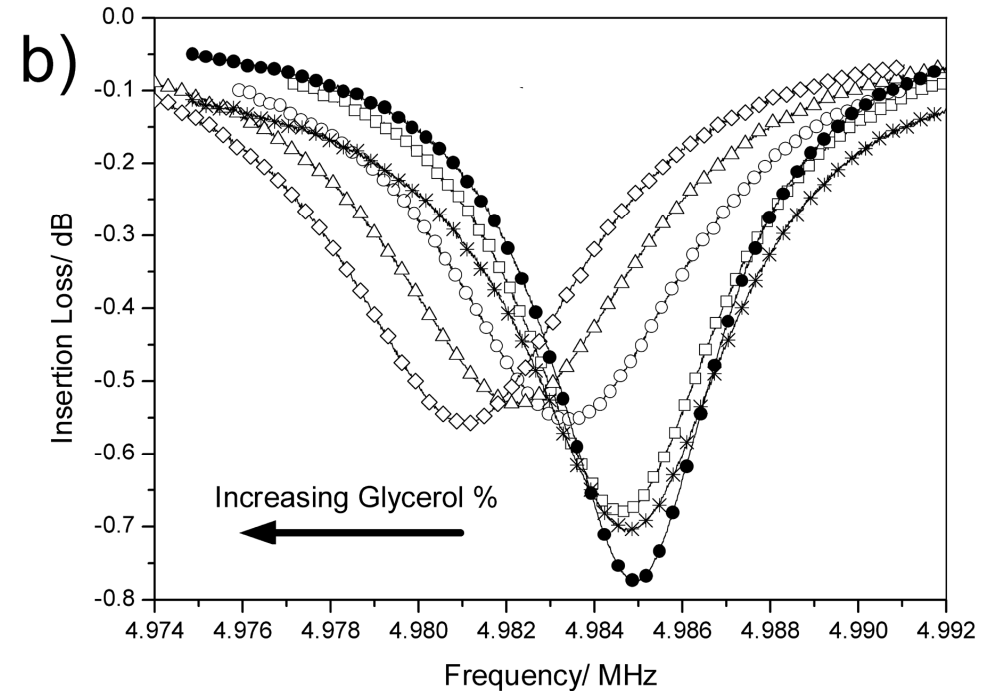
# QCM Spectra

## Hydrophobised 15 $\mu\text{m}$



Resonance sharpens with increasing viscosity-density

## Hydrophobised 18 $\mu\text{m}$



Frequency and bandwidth shifts are far less than K&G prediction



# Discussion Points?

## 1. Resonances

Length scales of features?

Compressional waves?

Penetration depth issues?

## 2. Types of Response

Viscoelasticity in air and/or in liquid?

Trapped “mass”, decoupling and slip?

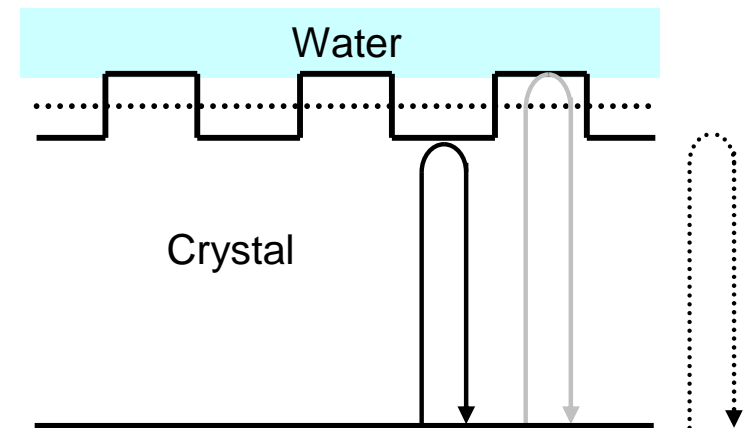
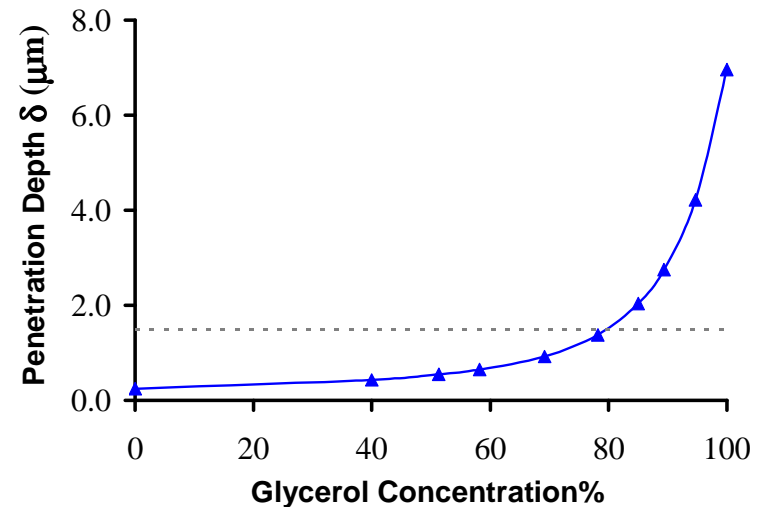
Sharpening resonances?

Positive frequency shifts?

## 3. Sensor Problems and Potential

Real surfaces are not polished crystals with fixed hydrophobicity

Design recognition layer that switches to hydrophilic on binding?



# Conclusions

## 1. Water/Glycerol on Micro-Posts

Bare/non-hydrophobised  $\Rightarrow$  Partial penetration of liquids

Hydrophobised  $\Rightarrow$  Superhydrophobic surfaces

## 2. Water/Glycerol Response of Micro-Post QCM's

Bare/non-hydrophobised  $\Rightarrow$  Newtonian-like response (conc<80%)

Hydrophobised  $\Rightarrow$  Change of type of response for height>5  $\mu\text{m}$

## 3. Unusual Responses for Hydrophobised Micro-Posts

All curves show a lower magnitude of response (decoupling)

Resonances can sharpen with increasing viscosity-density product

Tallest case (18  $\mu\text{m}$ ) shows most decoupling

Acknowledgements

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Engineering and Physical Sciences  
Research Council

**NOTTINGHAM**  
**TRENT UNIVERSITY**

# QCM: Slip Boundary Condition v Trapped Mass

- **Acoustic Impedance<sup>1</sup>**
  - Use slip length,  $b$ , and look at first order calculation

$$Z_L^{slip} \approx \frac{Z_L^{no\ slip}}{1 + \frac{b}{\eta_f} Z_L^{no\ slip}}$$

- **Newtonian Liquid<sup>2</sup>**
  - Kanazawa result for no-slip
  - Small “slip” correction uses  $b/\delta$

$$Z_L^{no\ slip} \approx \sqrt{i\omega\rho_f\eta_f}$$

$$\left(\frac{\Delta\omega}{\omega}\right)_{slip} \approx \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} \left(1 - \frac{2b}{\delta}\right)$$

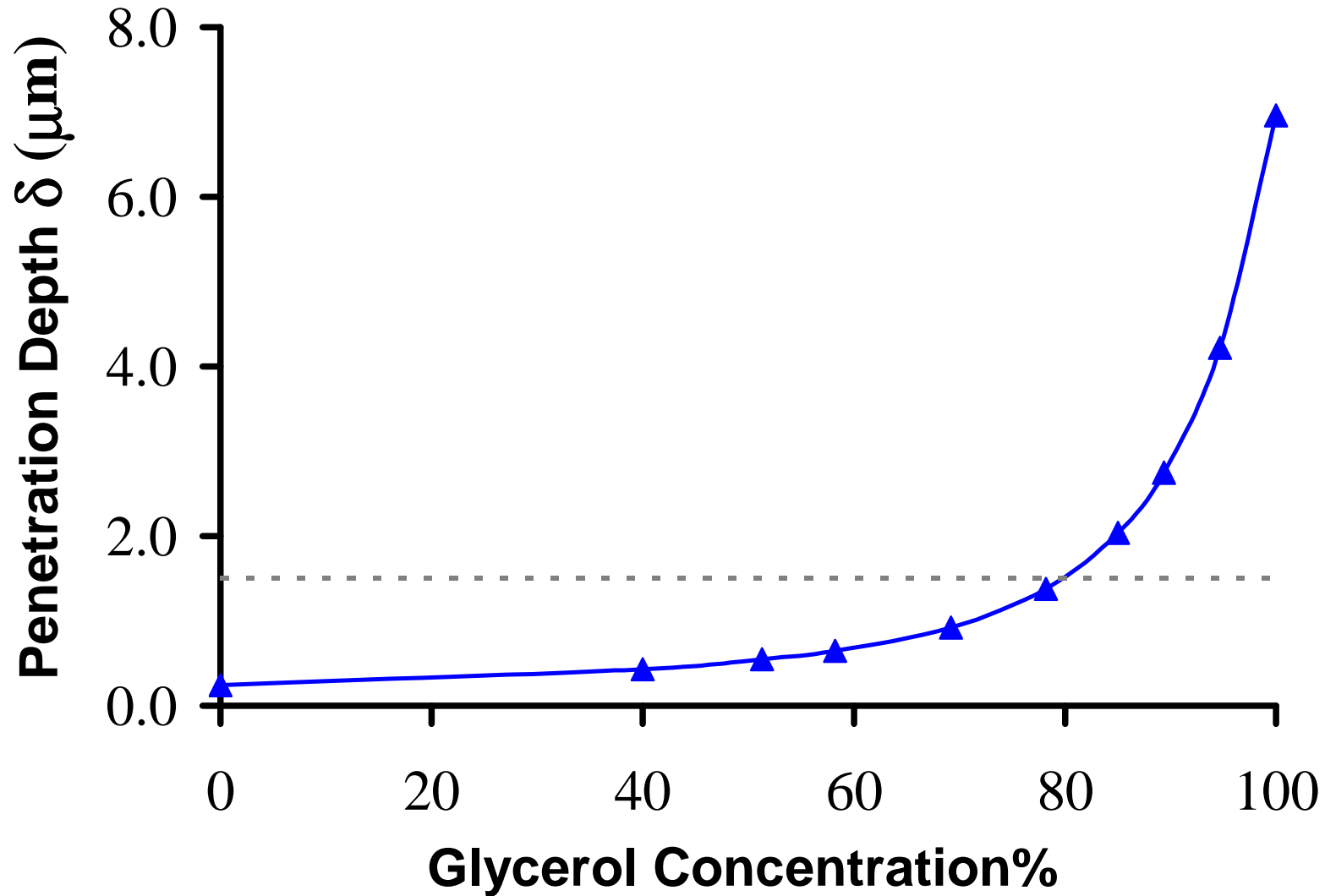
- **Negative  $b$  and Trapped Mass<sup>2,3</sup>**
  - Define a mass as  $\Delta m_f = b\rho_f$

“slip” correction

$$\left(\frac{\Delta\omega}{\omega}\right)_{additional} \approx \left(-\frac{2b}{\delta}\right) \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} = \frac{\omega\Delta m_f}{\pi\sqrt{\mu_s\rho_s}}$$

**Sauerbrey result for “rigid” liquid mass**

# Resonances with Penetration Depth

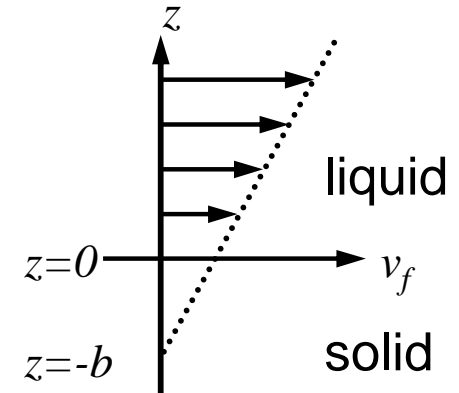


# “Slip” Boundary Condition v Trapped Mass

## Average Position of Solid-Liquid Interface

Slip length,  $b$ , to model average position of an interface

*Negative  $b \Rightarrow$  Effective interface moves to liquid side of boundary*



## Newtonian Liquid

Kanazawa & Gordon result for no-slip modified by “slip” correction using  $b/\delta$

$$\left(\frac{\Delta\omega}{\omega}\right)_{slip} \approx \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} \left(1 - \frac{2b}{\delta}\right)$$

Slip length to penetration depth

## Negative Slip Length

Define a mass as  $\Delta m_f = b\rho_f$

$$\left(\frac{\Delta\omega}{\omega}\right)_{additional} \approx \left(-\frac{2b}{\delta}\right) \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} = \frac{\omega\Delta m_f}{\pi\sqrt{\mu_s\rho_s}}$$

*Sauerbrey result for trapped “rigid” liquid mass*

# Acoustic Reflection View

## Substrate Supports Standing Waves



*Cavity length increases  $\Rightarrow$  additional frequency decrease*

## Limitations on “Slip” B.C./Trapped Mass View

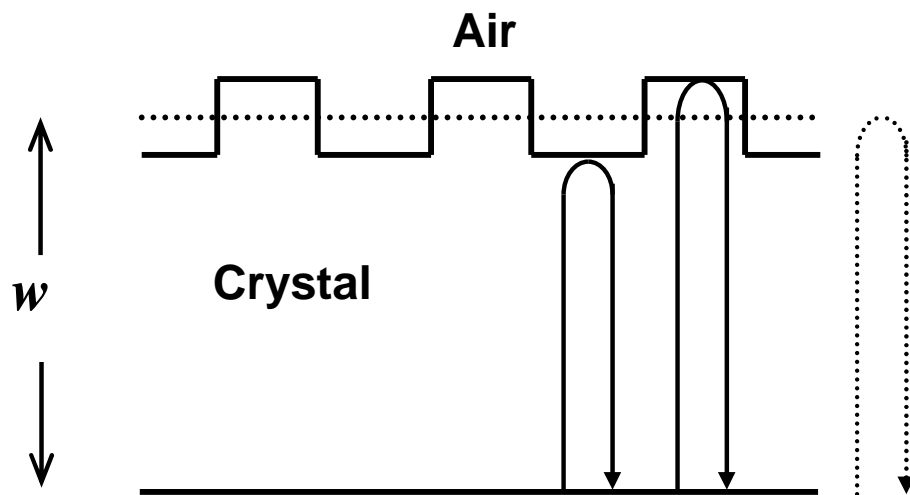
Effectively assuming equal reflectivity at peaks and troughs of topography

*Cannot necessarily use additivity of liquid entrainment + trapped mass when incomplete liquid penetration occurs*

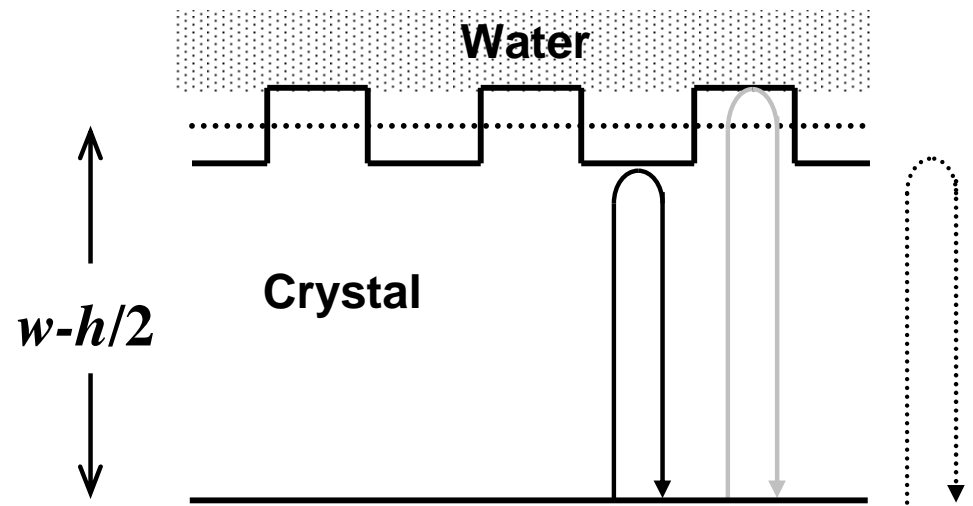
# A Mechanism for Positive Frequency Shifts?

- Effective Acoustic Cavity Length

- Air  $\Rightarrow$  top surface of crystal has uniform reflectivity
- Water  $\Rightarrow$  if air “trapping” occurs, reflectivity of peaks and troughs differs



Average cavity length exists

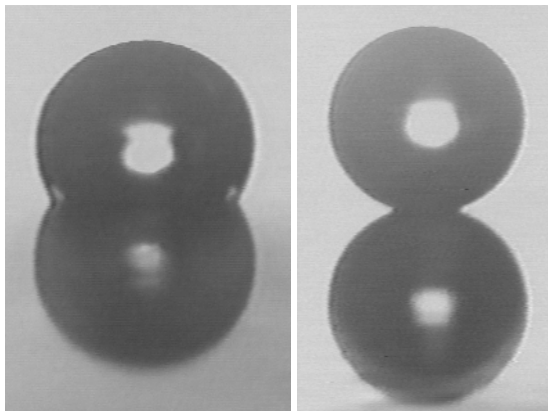
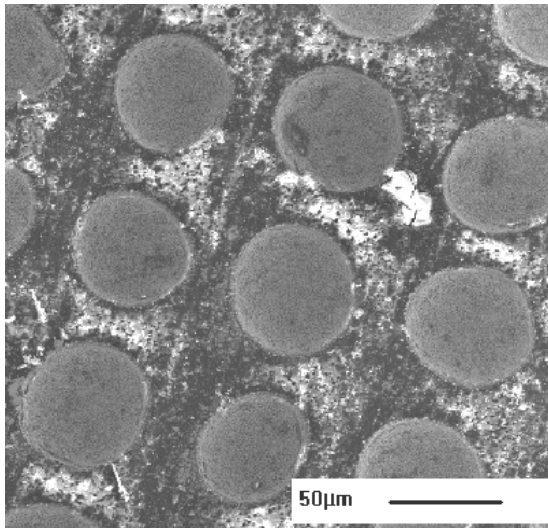


Average cavity length decreases

$$v=f\lambda \Rightarrow f \text{ increases}$$

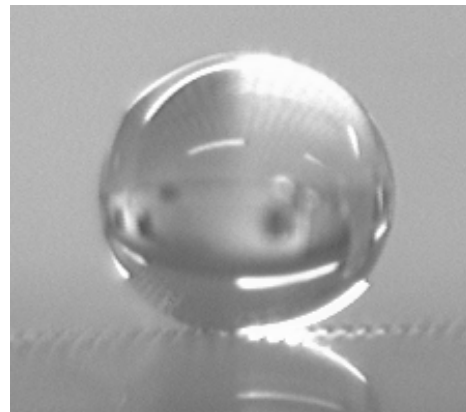
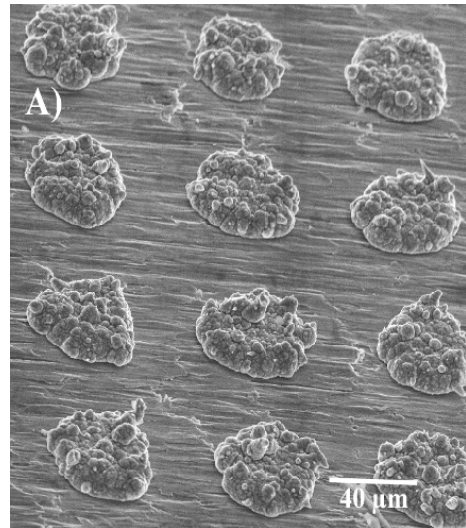
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## Etched Metal



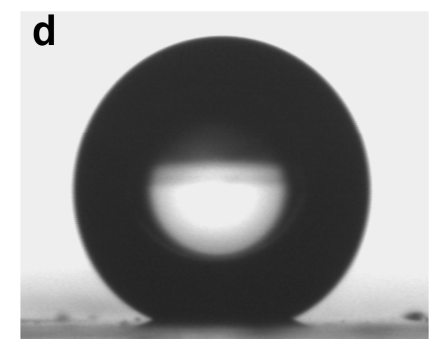
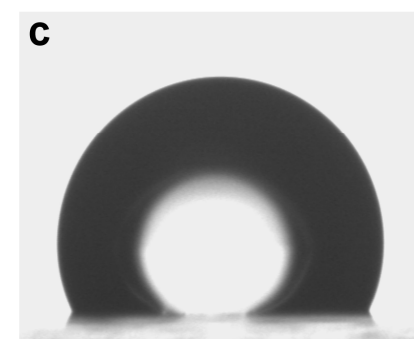
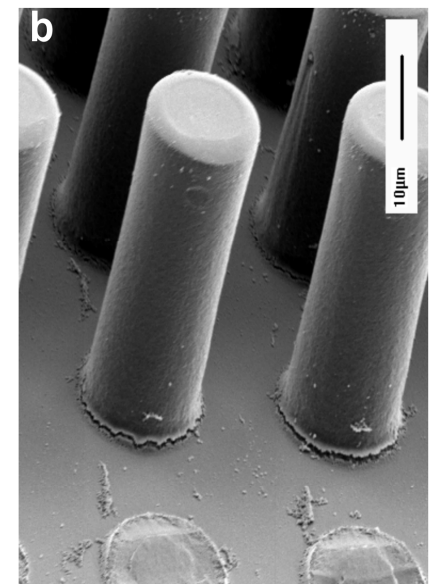
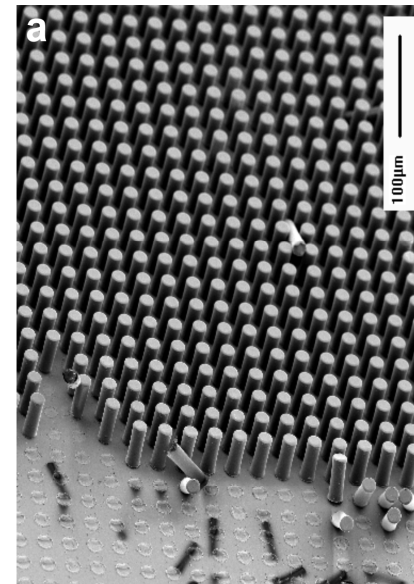
Flat & hydrophobic      Patterned & hydrophobic

## Deposited Metal



Patterned & hydrophobic

## Polymer Microposts



Flat & hydrophobic

Patterned & hydrophobic